## $7^{\text {th }}$ International Earth Science Olympiad

## Theoretical Test

Astronomy Model Answers

## A1. Atmosphere of Planets

See table: $\mathbf{+} \mathbf{0 . 5}$ points for each correct marking, $\mathbf{- 0 . 2}$ for each wrong marking.
A2. For winter solstice,

$$
\begin{aligned}
\mathrm{a}_{\mathrm{w}} & =90-\phi-\varepsilon \\
\mathrm{a}_{\mathrm{s}} & =180-(90-\phi+\varepsilon) \\
& =90+\phi-\varepsilon \\
\varepsilon & =23^{\circ} 26^{\prime} \\
\phi & =12^{\circ} 17^{\prime}
\end{aligned}
$$

Using these, Inclination of the Earth's axis,
(1.5 points for each of the four steps)

## A3. Pluto and charon:

(a) By Kepler's Third Law, $a_{0}^{3}=\frac{G\left(M_{p l}+M_{c h}\right) T^{2}}{4 \pi^{2}}=\frac{9 G M_{p l} T^{2}}{32 \pi^{2}}$

Hence $a_{0}=1.96 \times 10^{7} \mathrm{~m}$
(b) The distance of barycentre from Pluto will be $\mathrm{a}_{0} / 9$.
(1.5 points)

By comparing, a:b $=\frac{a}{b}=\frac{1.965 \times 10^{7}}{9 \times 1.195 \times 10^{6}}=1.83$
(1 point)
(1 points)
(c) One should try to resolve the Pluto-charon system, when the Pluto is closest to the Earth as thats when the angular separation will be highest.
( 0.5 point)
Let us say we are using optical wavelengths around 550 nm (a slightly better approximation will be to use blue end of visible light around 400 nm )

$$
\begin{equation*}
D=\frac{1.22 \lambda}{\theta}=\frac{1.22 \lambda d_{p l}}{a_{0}} \approx 15 \mathrm{~cm} \tag{1.5points}
\end{equation*}
$$

A4. H-R diagram
(a) Star of Largest Diameter
B Star of Smallest Diameter C
(2 points)
(b) $\mathbf{D}$ and $\mathbf{F}$
(c) $\mathbf{A}, \mathbf{E}$ and $\mathbf{F}$
(d) C

